

# Tracing the Base:

## A Topographic Test to Detect Collusive Basing-Point Pricing

by

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# Outline

- Introduction
- Competitive and Collusive Base Locations
- Tracing the Base
- A Topographic Test
- Concluding Remarks

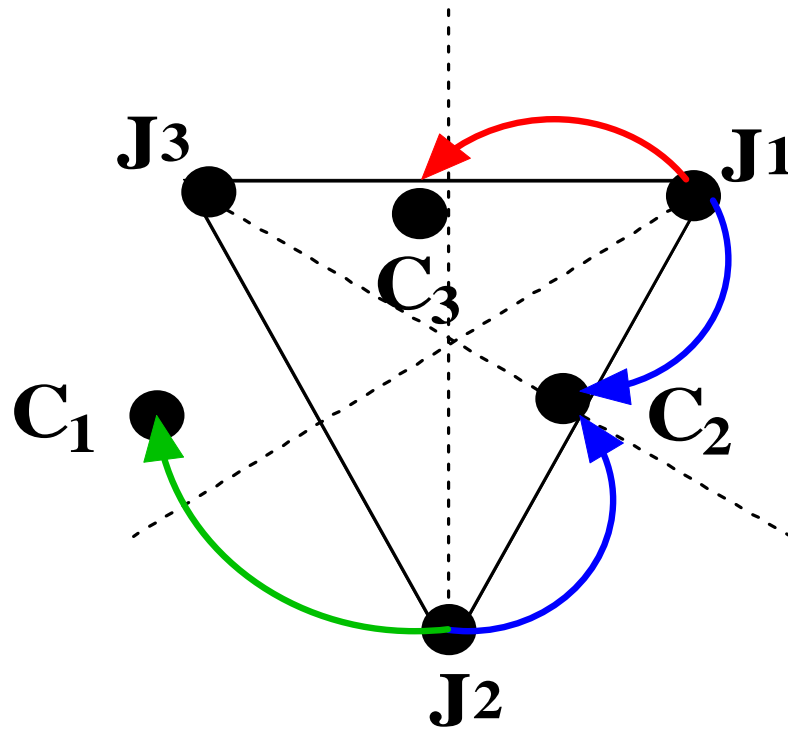


# Introduction

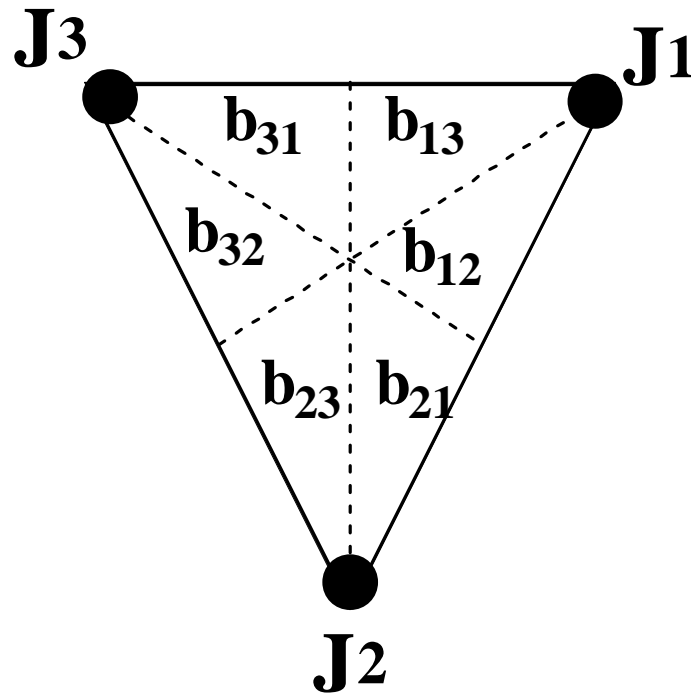
- BPP: “Prices quoted to buyers include transportation costs calculated from a given point of origin (the base-point), no matter where the product is actually shipped from” (Porter, 2005)
- What Type of Industries?
  - Homogeneous Bulky Products
  - Costly Transportation
  - Examples: Cement, Steel, Oil.
- BPP: Collusion or Competition?



# Competitive BPP with Three Firms



# Collusive BPP with Three Firms



⊕  
BP



# Tracing the Base

- Assuming linear bids:

$$p_i = cq_i + t(l_j - x_i)$$

- Known: price ( $p$ ), quantity ( $q$ ) and consumer location ( $x$ ).
- To recover: costs ( $c$  and  $t$ ) and the Base-Point ( $l$ ) that is used.



# Tracing the Base

- Coordinates  $(\mathbf{a}, \mathbf{b})$
- Distance follows from Pythagoras' Law:

$$(l_j - x_i)^2 = (\mathbf{a}_j - \mathbf{a}_i)^2 + (\mathbf{b}_j - \mathbf{b}_i)^2$$

- Substituting yields:

$$p_i = cq_i + t\sqrt{(\mathbf{a}_j - \mathbf{a}_i)^2 + (\mathbf{b}_j - \mathbf{b}_i)^2}$$



# Tracing the Base

- Normalize transportation costs to one and rewriting yields:

$$\mathbf{a}_j = \mathbf{a}_1 \pm \sqrt{(p_1 - cq_1)^2 - (\mathbf{b}_1 - \mathbf{b}_j)^2}$$

$$\mathbf{a}_j = \mathbf{a}_2 \pm \sqrt{(p_2 - cq_2)^2 - (\mathbf{b}_2 - \mathbf{b}_j)^2}$$

$$\mathbf{a}_j = \mathbf{a}_3 \pm \sqrt{(p_3 - cq_3)^2 - (\mathbf{b}_3 - \mathbf{b}_j)^2}$$

- Solve numerically





# Tracing the Base

- What happens if BPP is competitive?
- Apply algorithm for all pairs of three consumers
- Output: locations of firms
- Take weighted average in order to construct artificial candidate base, which is always situated in the convex hull.



# A Topographic Test

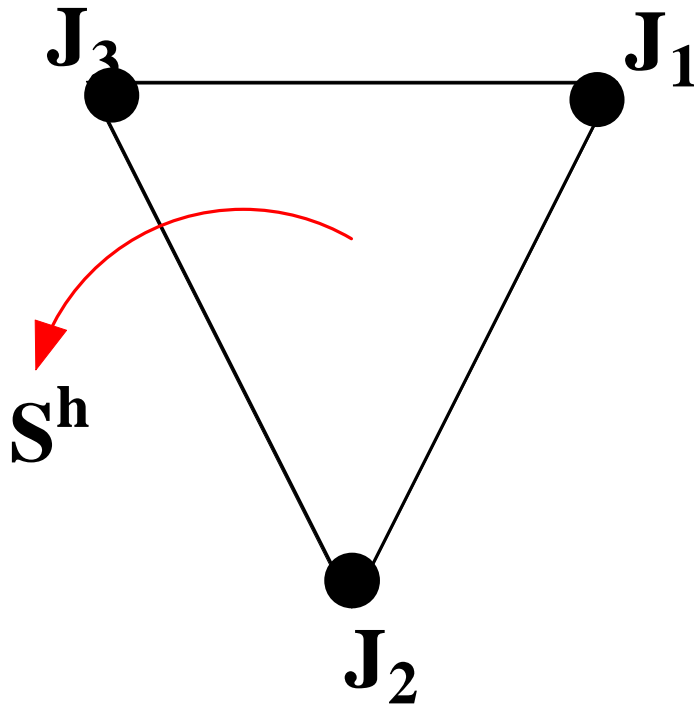
- Competitive BP:  $(\mathbf{a}^{BP}, \mathbf{b}^{BP}) \pm 2 \times \sqrt{\frac{\sum_{k=1}^K (\mathbf{a}^{BP} - \mathbf{a}_k)^2 + \sum_{k=1}^K (\mathbf{b}^{BP} - \mathbf{b}_k)^2}{K}}$
- Collusive BP:  $(\mathbf{a}^{BP}, \mathbf{b}^{BP})$
- CBP-Measure:

$$CBP = 1 - \frac{S^* \cap S^h}{S^h} \in [0,1]$$

- Collusion:  $CBP = 1$
- Competition:  $CBP = [0,1)$



# Collusive BPP

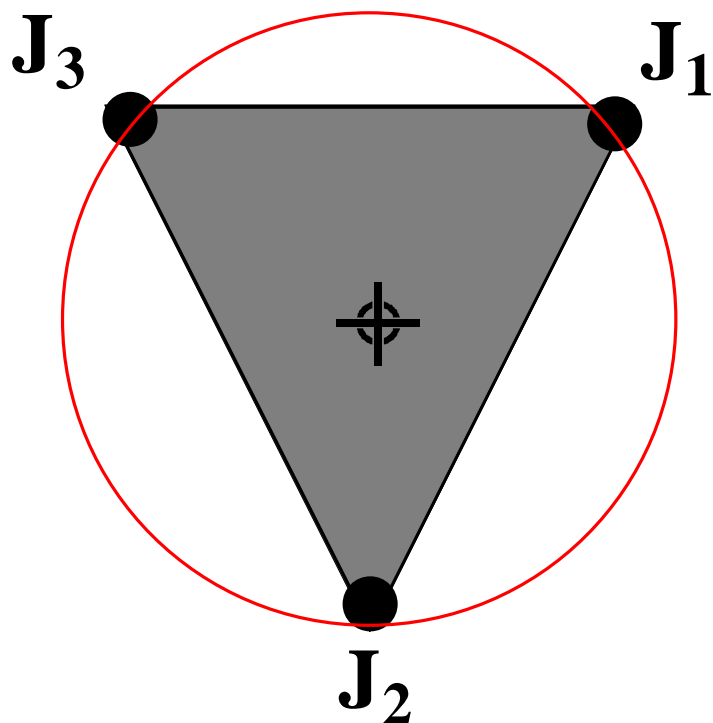


$$CBP = 1 - \frac{S^* \cap S^h}{S^h} = 1 - \frac{0}{S^h} = 1$$

$\oplus$   
BP



# Competitive BPP



$$CBP = 1 - \frac{S^* \cap S^h}{S^h} = 1 - \frac{S^h}{S^h} = 0$$



# Concluding Remarks

- A Cartel Detection Method:
  - Industries that are *a priori* vulnerable to price conspiracies
  - Discriminates between competitive and collusive situations
  - Relatively cheap to implement (categories: G, Y, R)
  - Costly to beat
- Measurement errors
- Different bid structures
- Longitude, latitude and altitude
- A detection software

